

Confinement slingshot and gravitational waves

Gravitational Wave Probes of Physics Beyond the Standard Model
Michael Zantedeschi



李政道研究所
TSUNG-DAO LEE INSTITUTE

Based on:

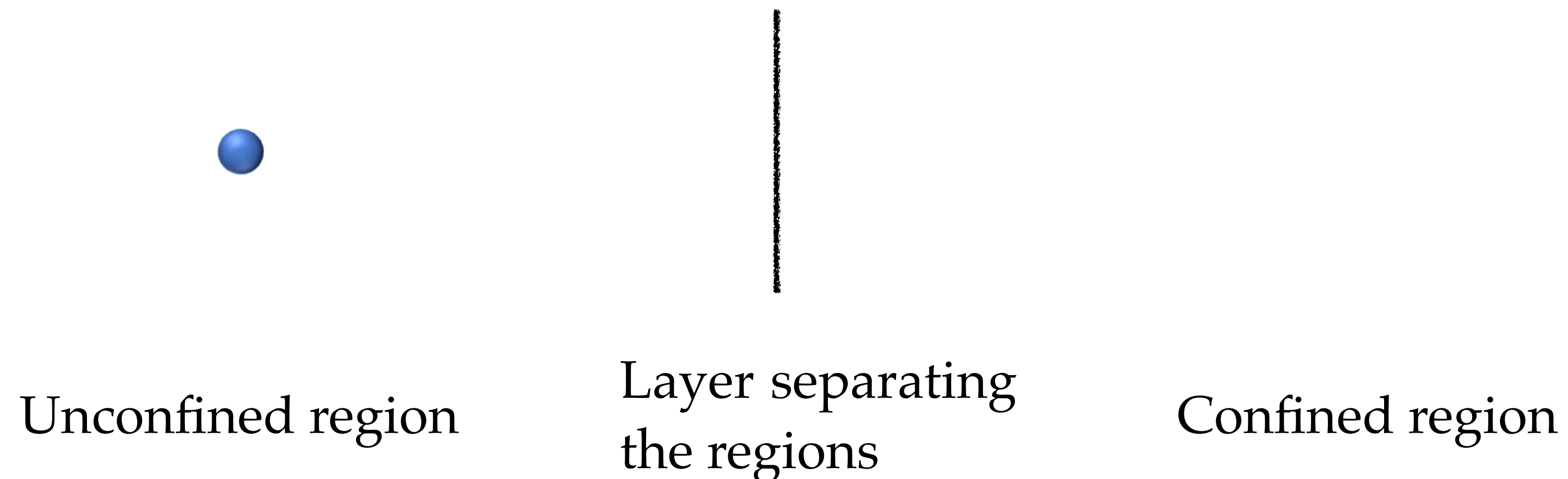
Dvali, Kühnel, MZ, [2108.09471](#)

Dvali, Bermudez-Valbuena, MZ, [2210.14947](#)

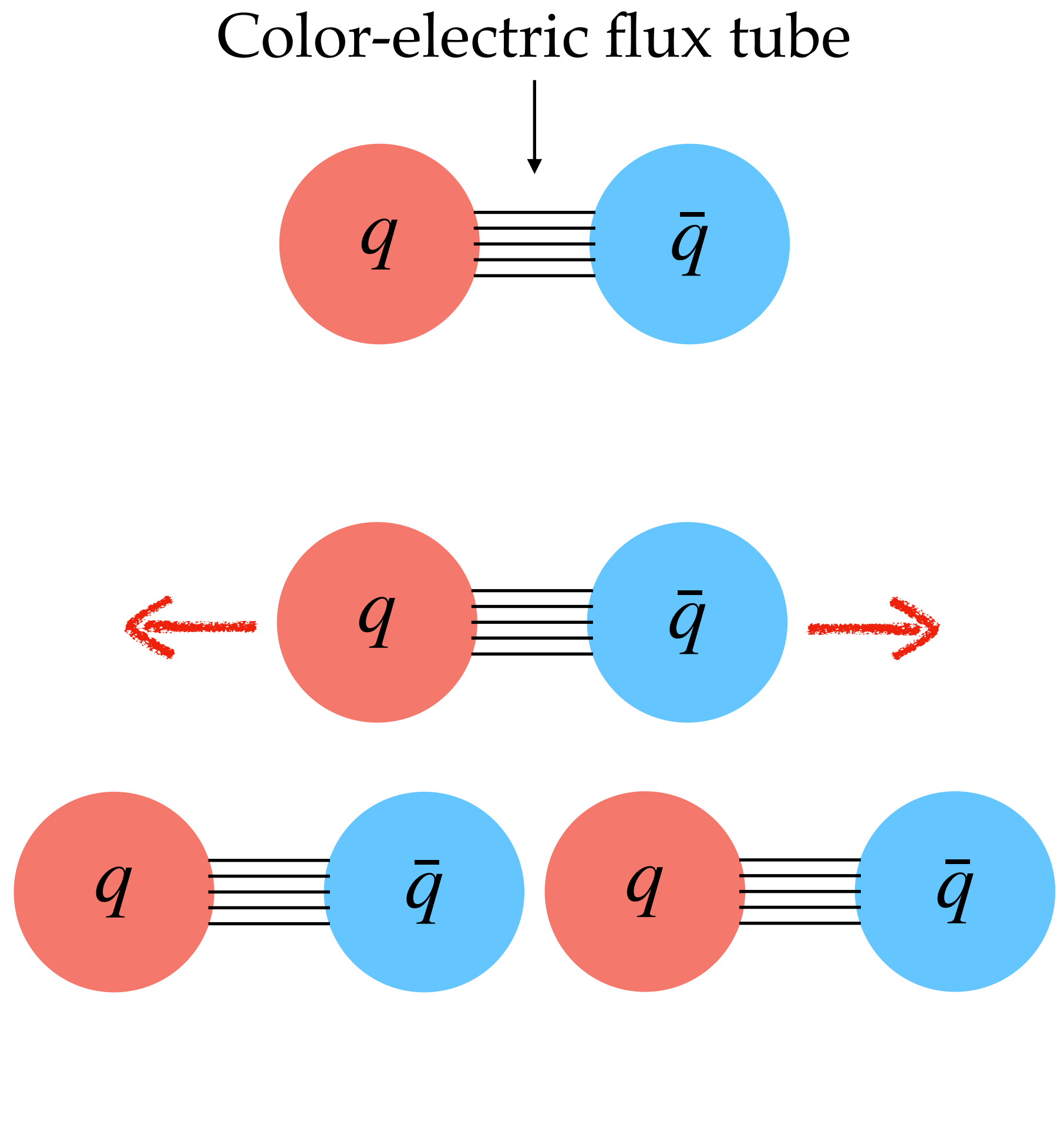
Dvali, Bachmaier, Bermudez-Valbuena, MZ, [2309.14195](#)

Motivation and Goal

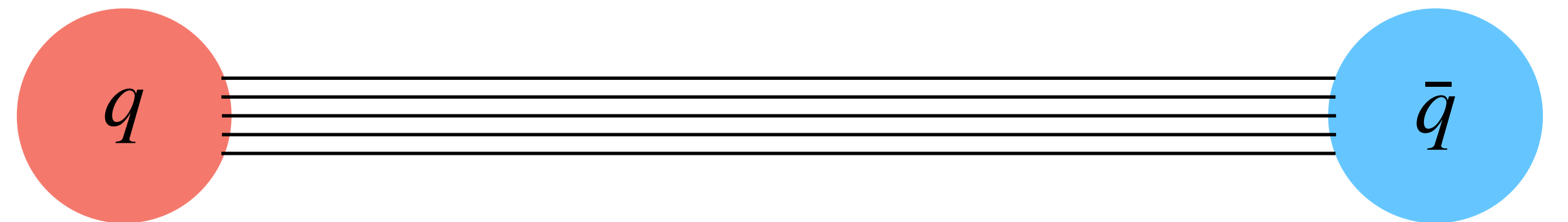
- Understanding the transition between the confining and deconfining regimes of gauge theories in a controllable environment
- The coexistence of confining and unconfined vacua is realised in several beyond Standard Model extensions (e.g., intermediate scales of Grand unified theories, branes).
- Confinement forces a specific dynamics, leading to the production of gravitational waves.



Confinement



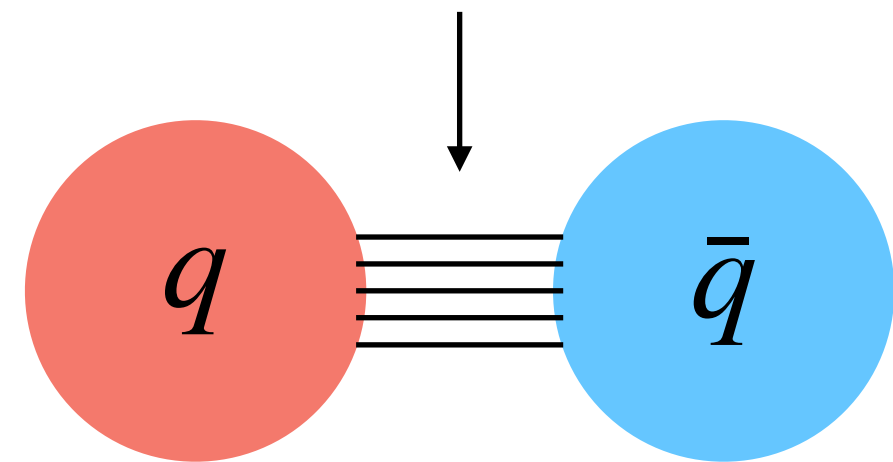
- Colour-charged particles (quarks and gluons) cannot be isolated. States are colourless below the confinement scale Λ_c
- Flux tubes of colour (strings) connect quarks
- Property of gauge theories (e.g., QCD)
- Separating quarks \rightarrow nucleation of pairs
- $P_{\text{tunnel}} \propto e^{-\pi \left(M_q / \Lambda_c \right)^2} \rightarrow$ if $M_q > \Lambda_c$ we could stretch an exponentially long string



Confinement

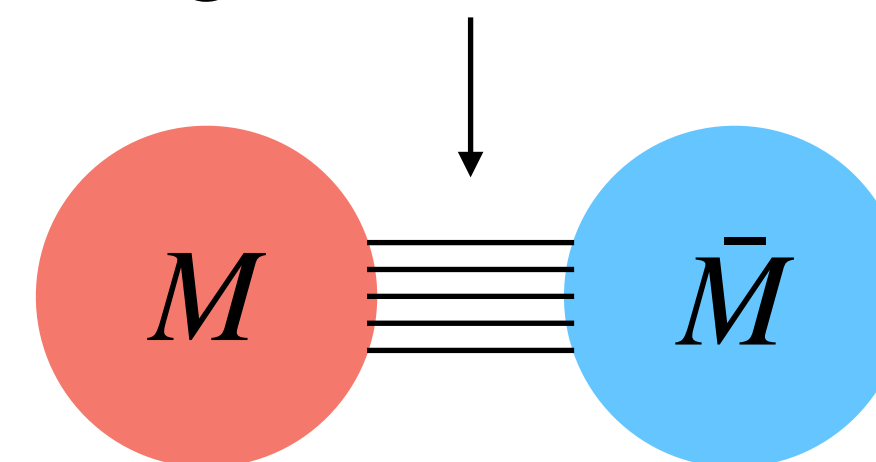
There is a duality between colour electric confinement and magnetic confinement
Dvali, Vilenkin hep-th/0209217

Color-electric flux tube



- strongly coupled
- quantum system

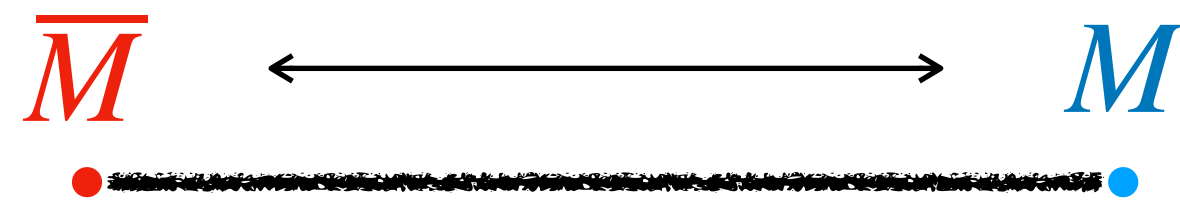
Magnetic flux tube



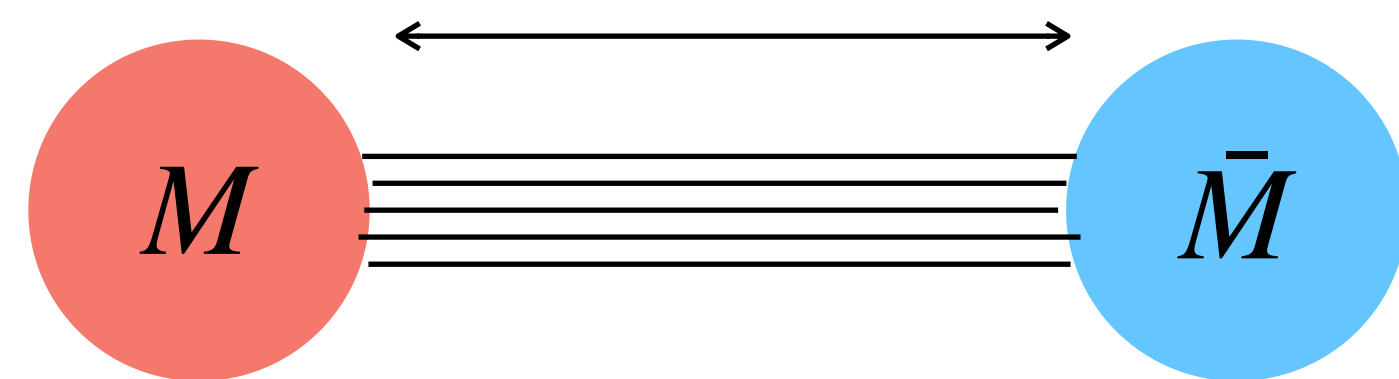
- weakly coupled
- admits classical description
- confinement is realised by Higgsing
- Realisation in terms of confined 't Hooft Polyakov monopoles

Confinement

Point-like limit previously studied by *Martin, Vilenkin '96*



$$S = - m_M \int ds_1 - m_M \int ds_2 - \Lambda^2 \int d\Sigma$$



- Which admits solution of constantly accelerating, oscillating monopoles, with $a = \Lambda^2/m_M$

- Gravitational radiation with power

$$P_n \sim \frac{G_N \Lambda_c^4}{n}, \quad \omega_n = 2\pi n/d,$$

We looked at this in an explicit realisation with 't Hooft Polyakov monopoles

Dvali, Bermudez-Valbuena, MZ, [2210.14947](#)

System

$$\mathcal{L} = \text{Tr} \left((D_\mu \phi)^\dagger (D^\mu \phi) \right) + (D_\mu \psi)^\dagger (D^\mu \psi) - \frac{1}{2} \text{Tr} \left(G^{\mu\nu} G_{\mu\nu} \right) - U(\phi, \psi)$$

$$U(\phi, \psi) = U(\phi) + U(\psi) + \beta \psi^\dagger \phi \psi$$

The system consists of a scalar adjoint, which provides monopole solution, and a scalar doublet, which makes the residual U(1) massive, leading to monopole confinement

SU(2) adjoint

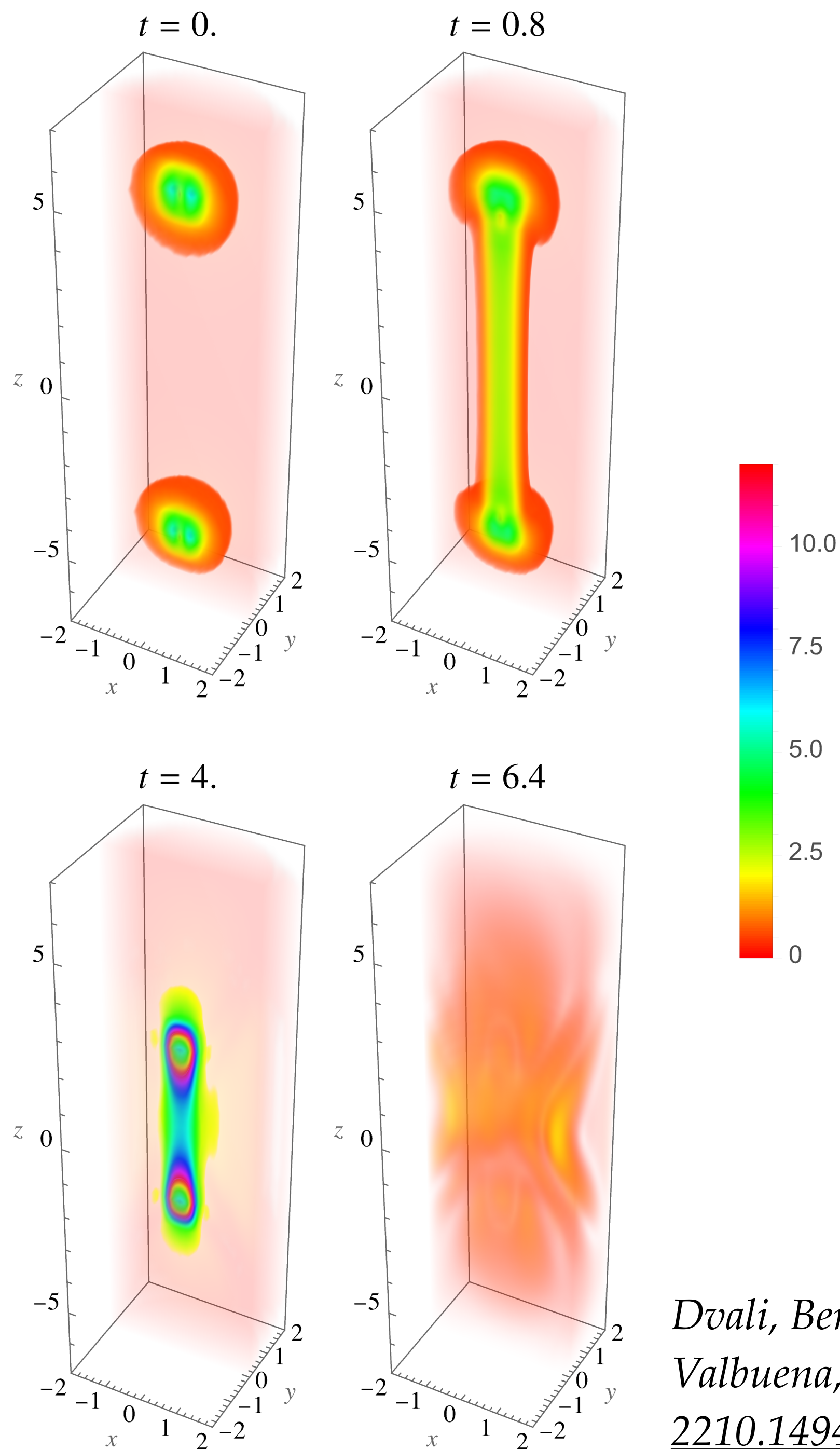
SU(2) doublet

$$SU(2) \xrightarrow{\langle v_\phi \rangle} U(1) \xrightarrow{\langle v_\psi \rangle} 1$$

Massive "W[±]"

Massive "A"

Dynamics

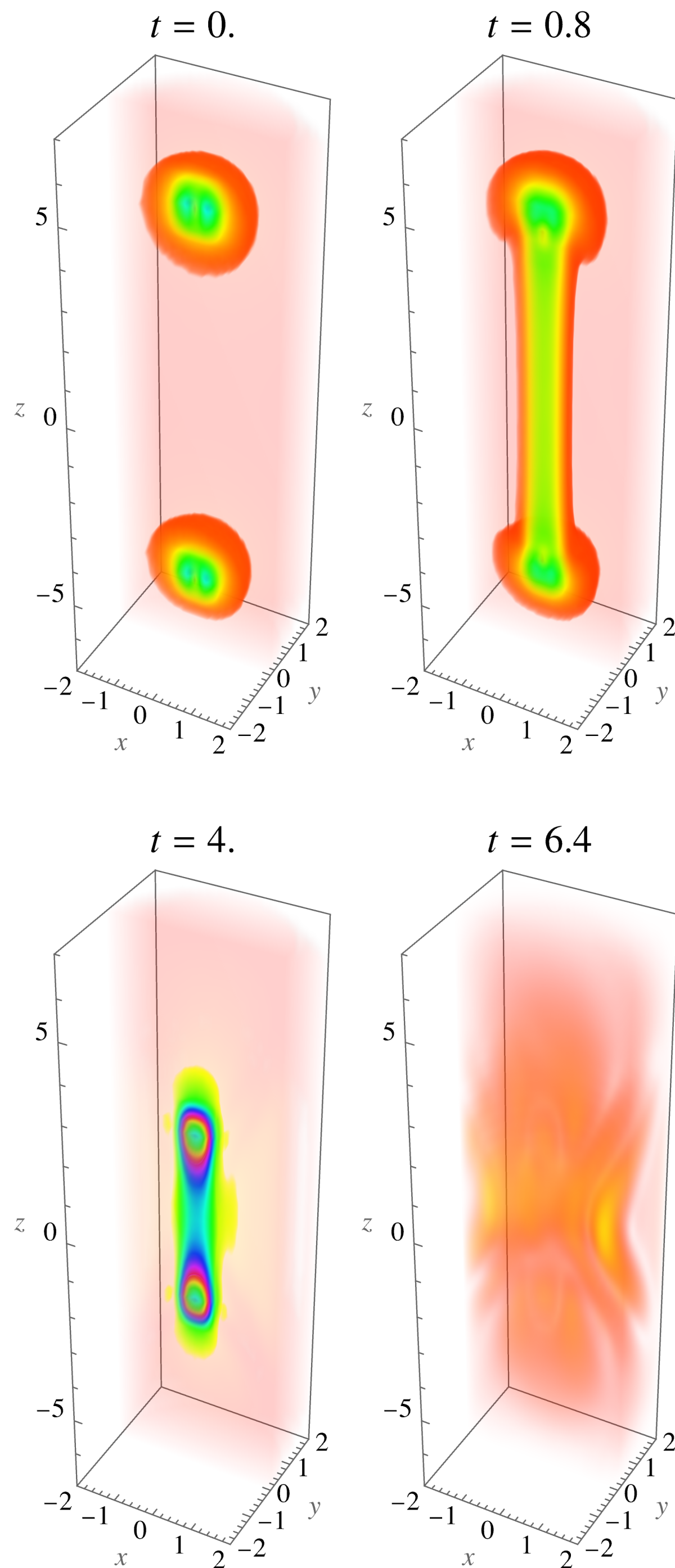


- Monopole-antimonopole pairs in confined region: their magnetic charge is confined into a string connecting them
- Energy stored in the string, given by $E \sim \Lambda^2 d$, is transferred to the kinetic energy of the monopoles which are constantly accelerated towards each other with $a = \Lambda^2/m$ and eventually annihilates
- System now simply annihilates and does not oscillate as opposed to point-like case
- New possibilities: the monopole can be twisted with respect to the antimonopole. In the maximal 'twist' case, the configuration is a microscopic realization of a sphaleron

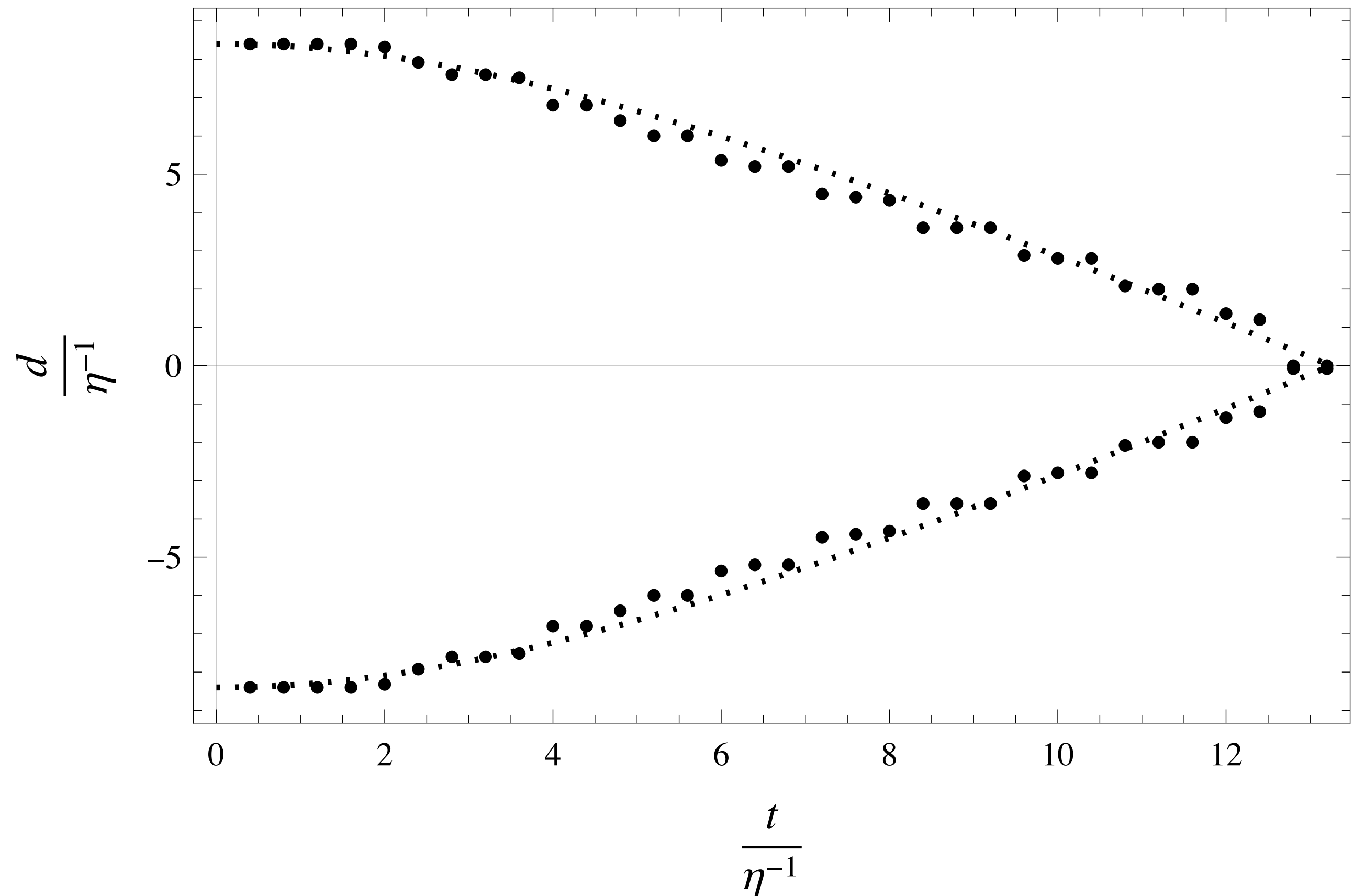
Dvali, Bermudez-Valbuena, MZ,
[2210.14947](https://arxiv.org/abs/2210.14947)

Dynamics

The dynamics is compatible with the one of constantly accelerating relativistic particles with $a = \Lambda^2/m$

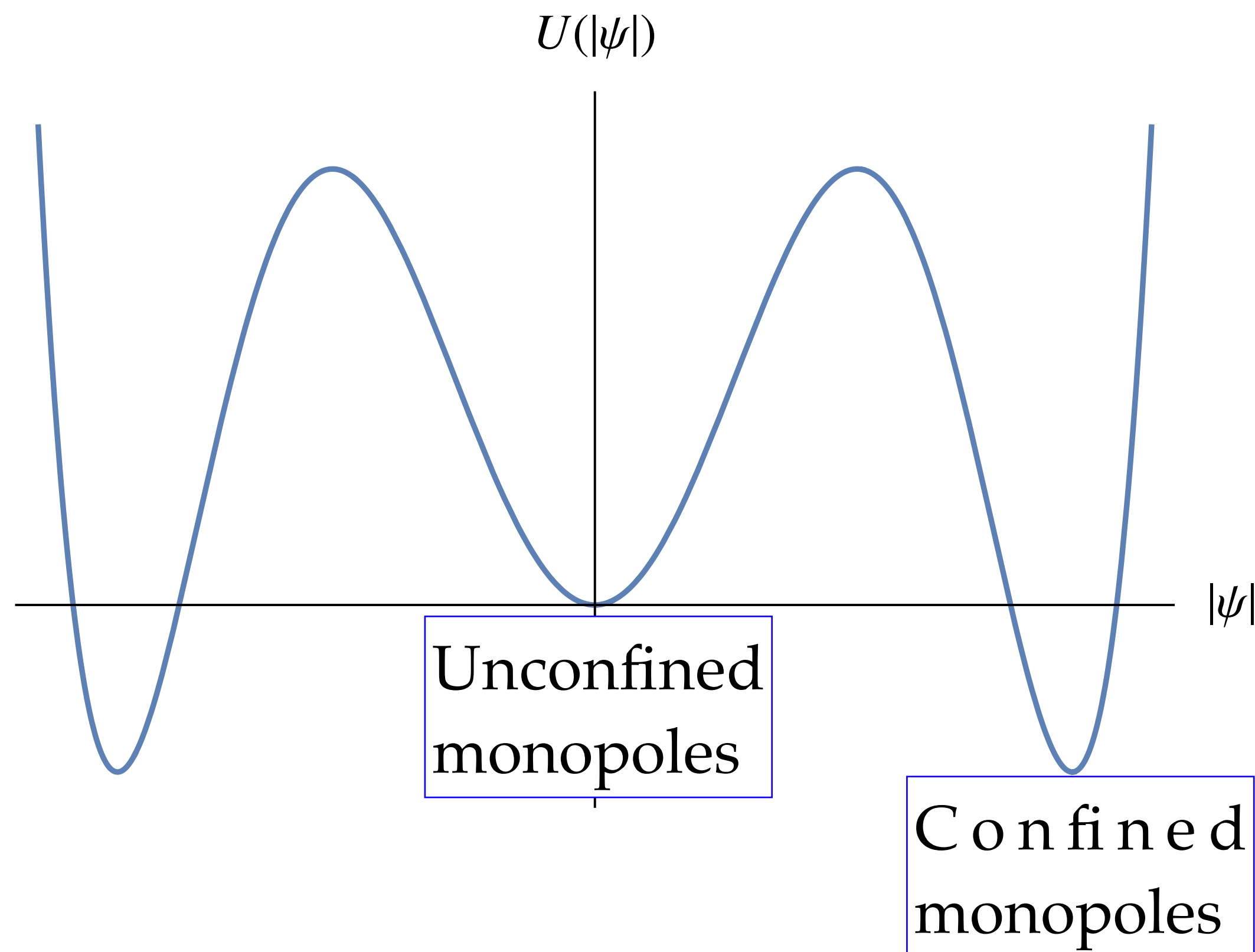


Dvali, Bermudez-Valbuena, MZ, 2210.14947



Confined - unconfined layer

Coexistence of confining and unconfining phase is realised if ψ undergoes a first order phase transition



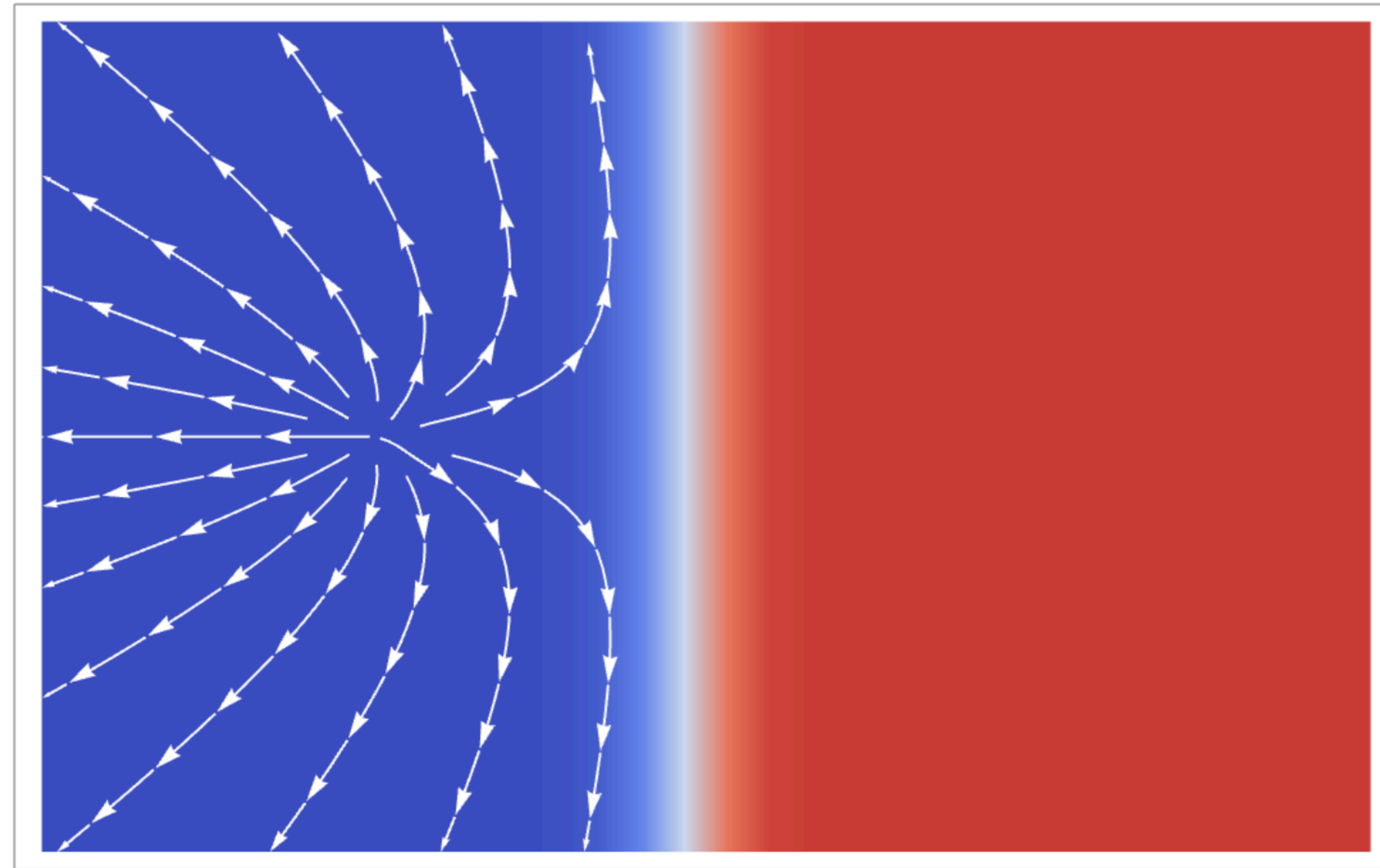
- The potential is typically realised by taking into account thermal corrections in the early Universe
- $\langle \psi \rangle = 0$ corresponds to the unconfined region
- $\langle \psi \rangle = v_\psi$ breaks the U(1) and confines the monopoles
- The system admits (unstable) domain walls (layer) interpolating between the two

Slingshot setup

Dvali, Bachmaier, Bermudez-Valbuena, MZ, [2309.14195](#)

$$\vec{B}(x, z, y = 0)$$

Unconfined region
(Coulomb region)
“Photon” is massless



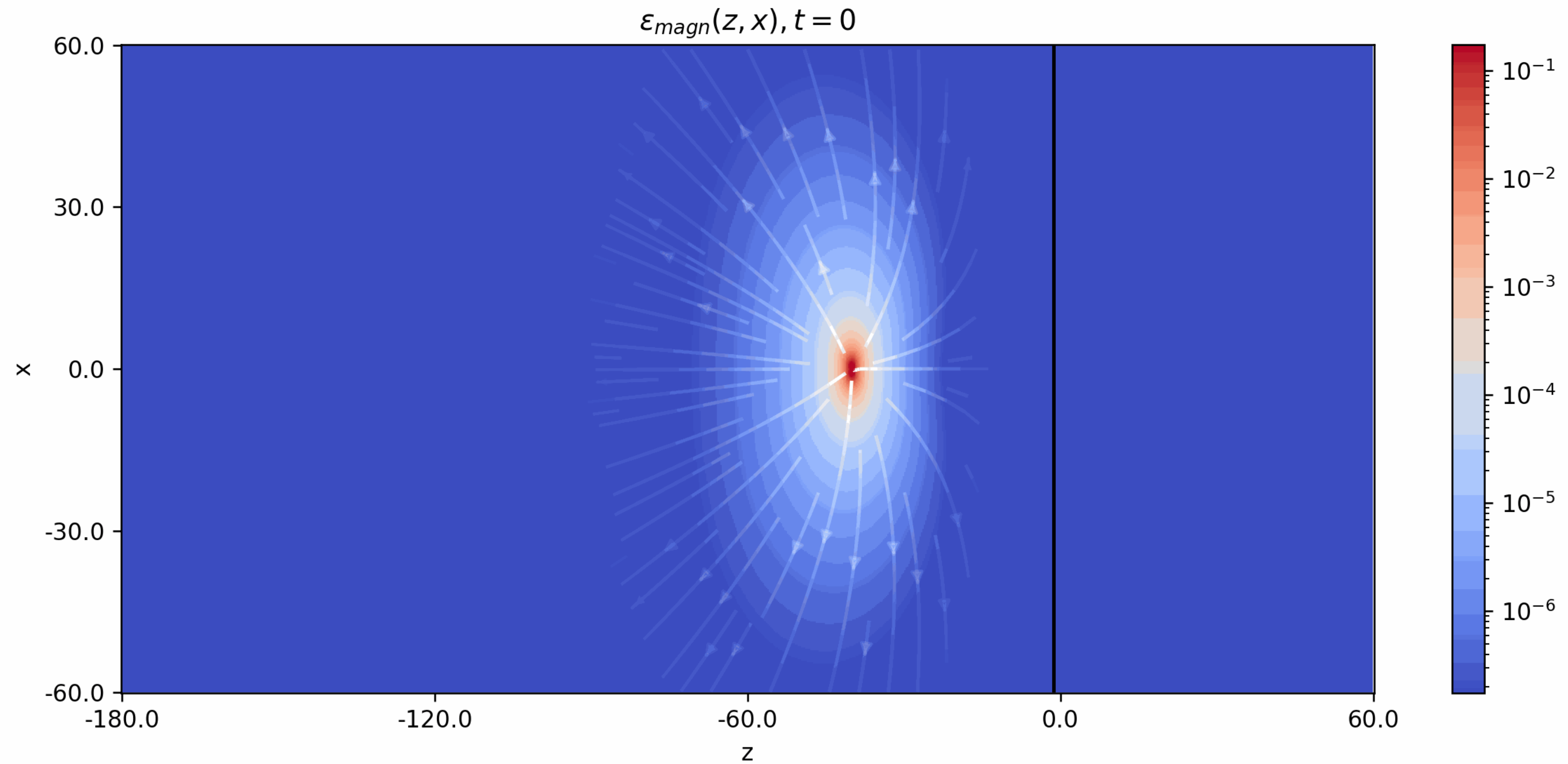
Confined region
(Higgsed region)
“Photon” is massive

Layer separating
the regions

Monopole starts in unconfined region and display a Coulomb-like magnetic field. At the layer interface, the magnetic lines are repelled, analogously to Meissner effect.

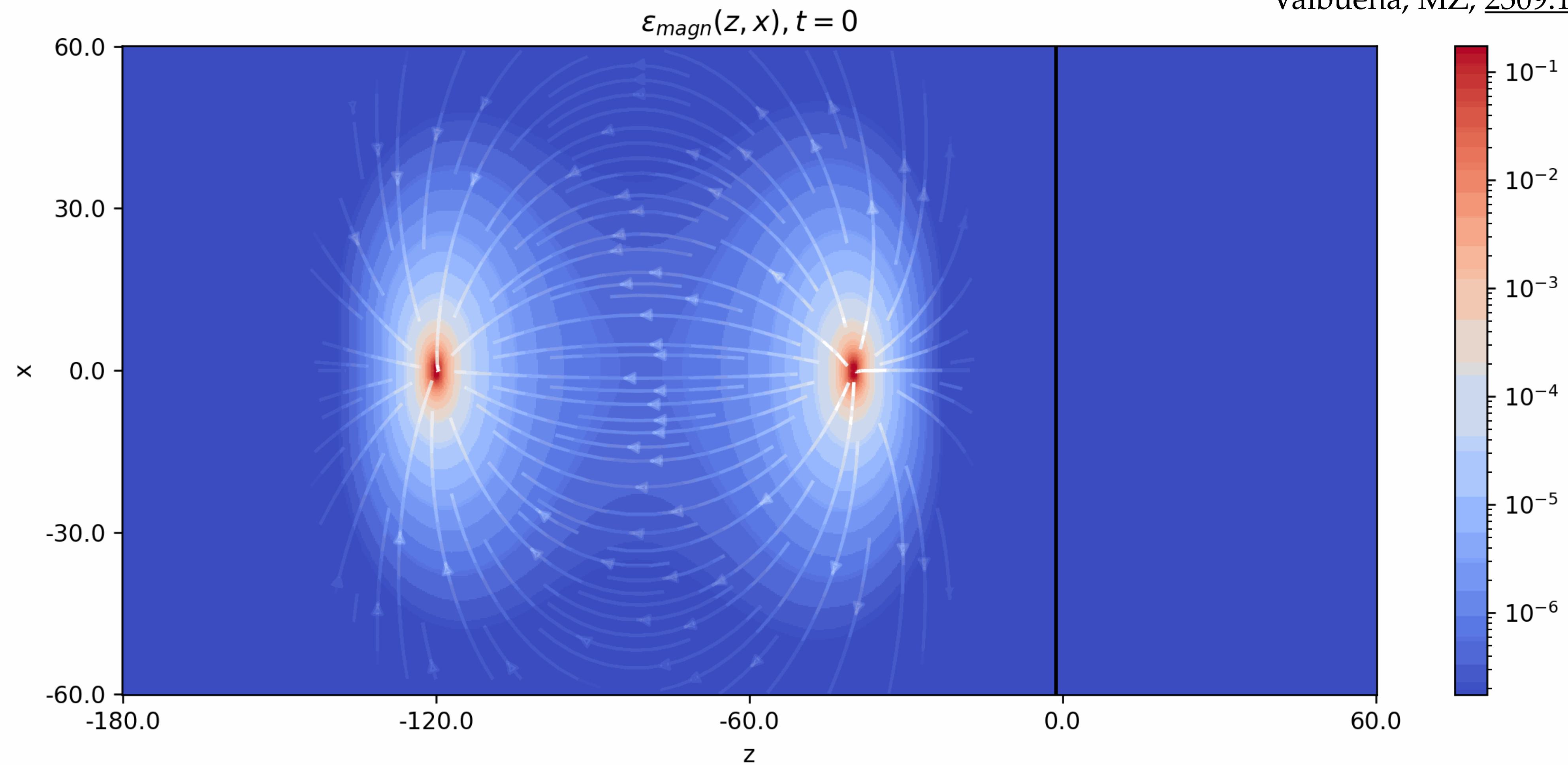
Slingshot Dynamics

Dvali, Bachmaier, Bermudez-Valbuena, MZ, [2309.14195](#)



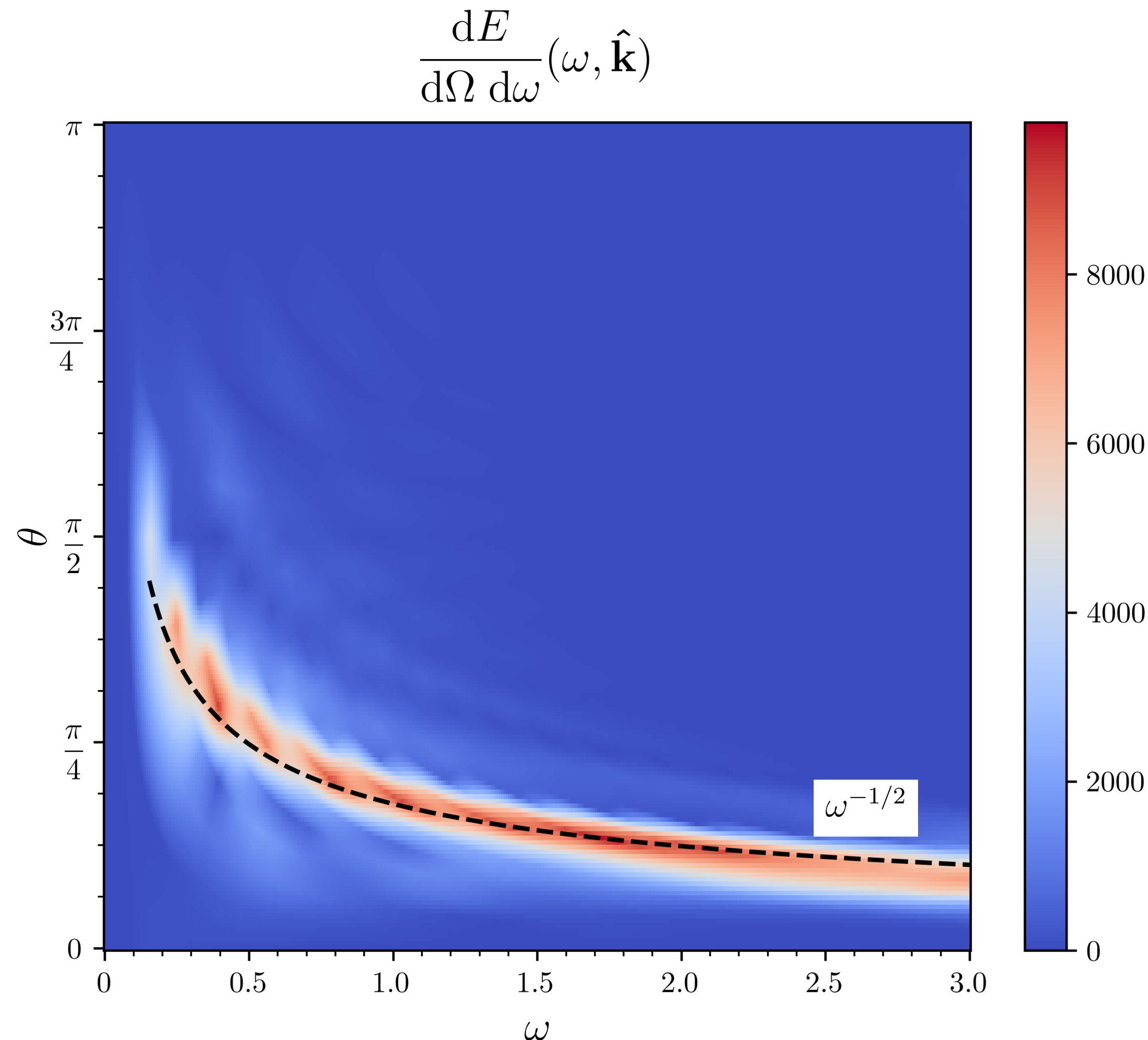
Dynamics monopole-antimonopole

Dvali, Bachmaier, Bermudez-Valbuena, MZ, [2309.14195](#)



Gravitational Waves from Slingshot

Dvali, Bachmaier, Bermudez-Valbuena, MZ, [2309.14195](#)



$$\frac{dE_n}{d\Omega d\omega} = \frac{G \omega_n^2}{\pi} \left(T_{\mu\nu}^*(\omega_n, \mathbf{k}) T^{\mu\nu}(\omega_n, \mathbf{k}) - \frac{1}{2} |T_\mu^\mu(\omega_n, \mathbf{k})|^2 \right)$$

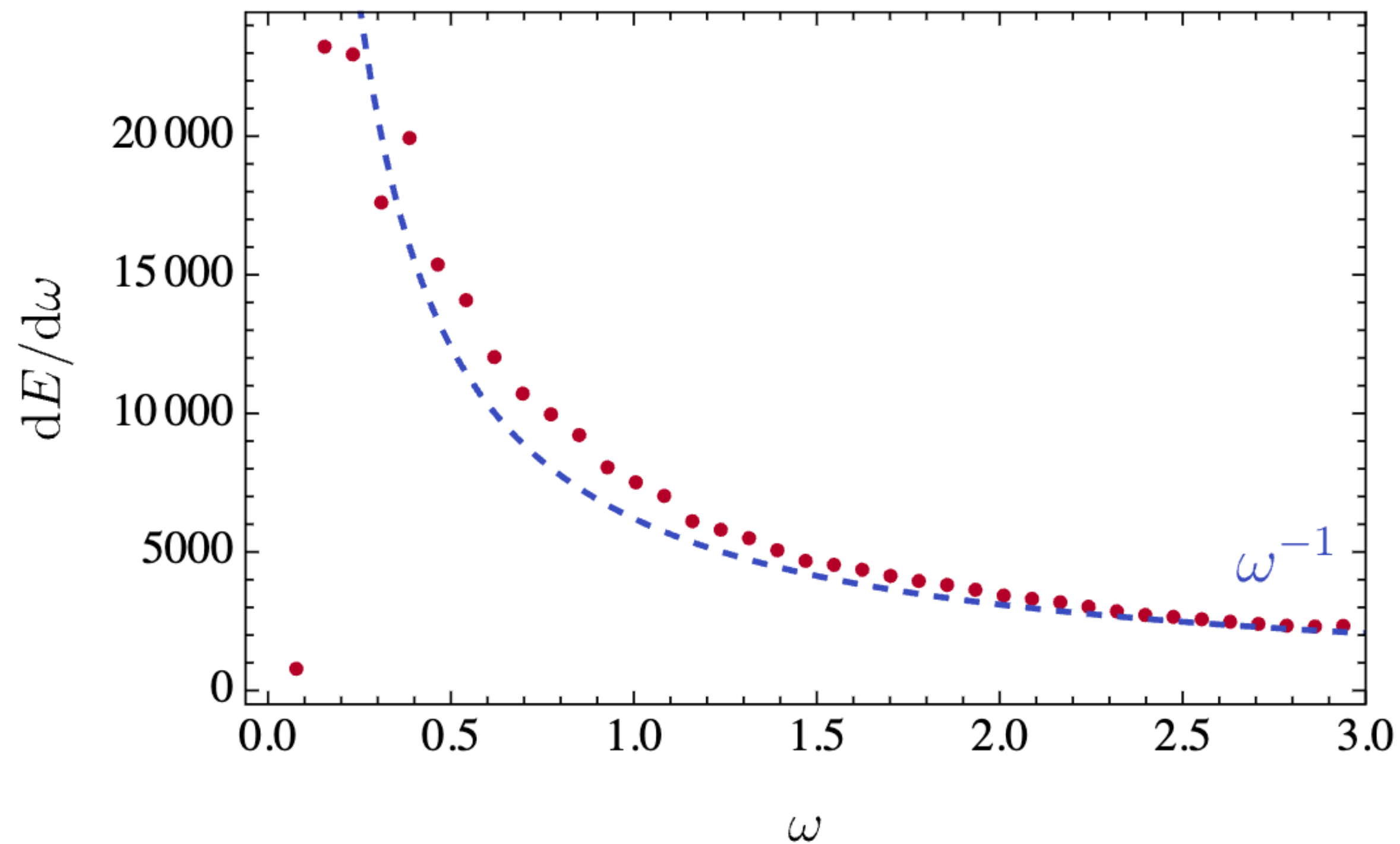
Emission takes place in a beaming angle with scaling

$$\theta \propto \omega^{-1/2}$$

This is typical behaviour of monopole accelerated by a string, as found, in the point-like analysis of a monopole-antimonopole pair connected by a string *Martin, Vilenkin '96 + Leblond, Shlaer, Siemens '09*

Gravitational Waves from Slingshot

Dvali, Bachmaier, Bermudez-Valbuena, MZ, [2309.14195](#)



Angularly integrated spectrum scales approximately as

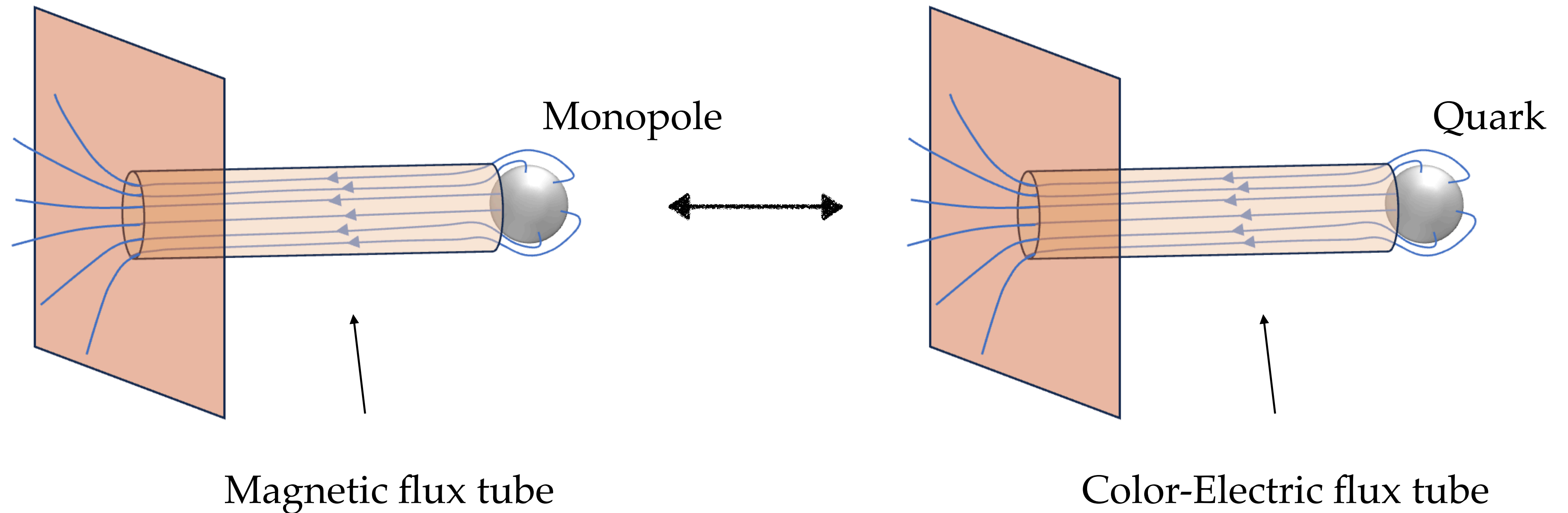
$$\frac{dE}{d\omega} \propto \omega^{-1}$$

This is analogous to the behaviour we found for a confined monopole-antimonopole pair previously mentioned.

More in general we get $P_n = G_N \Lambda_c^4 / n$

Dual picture

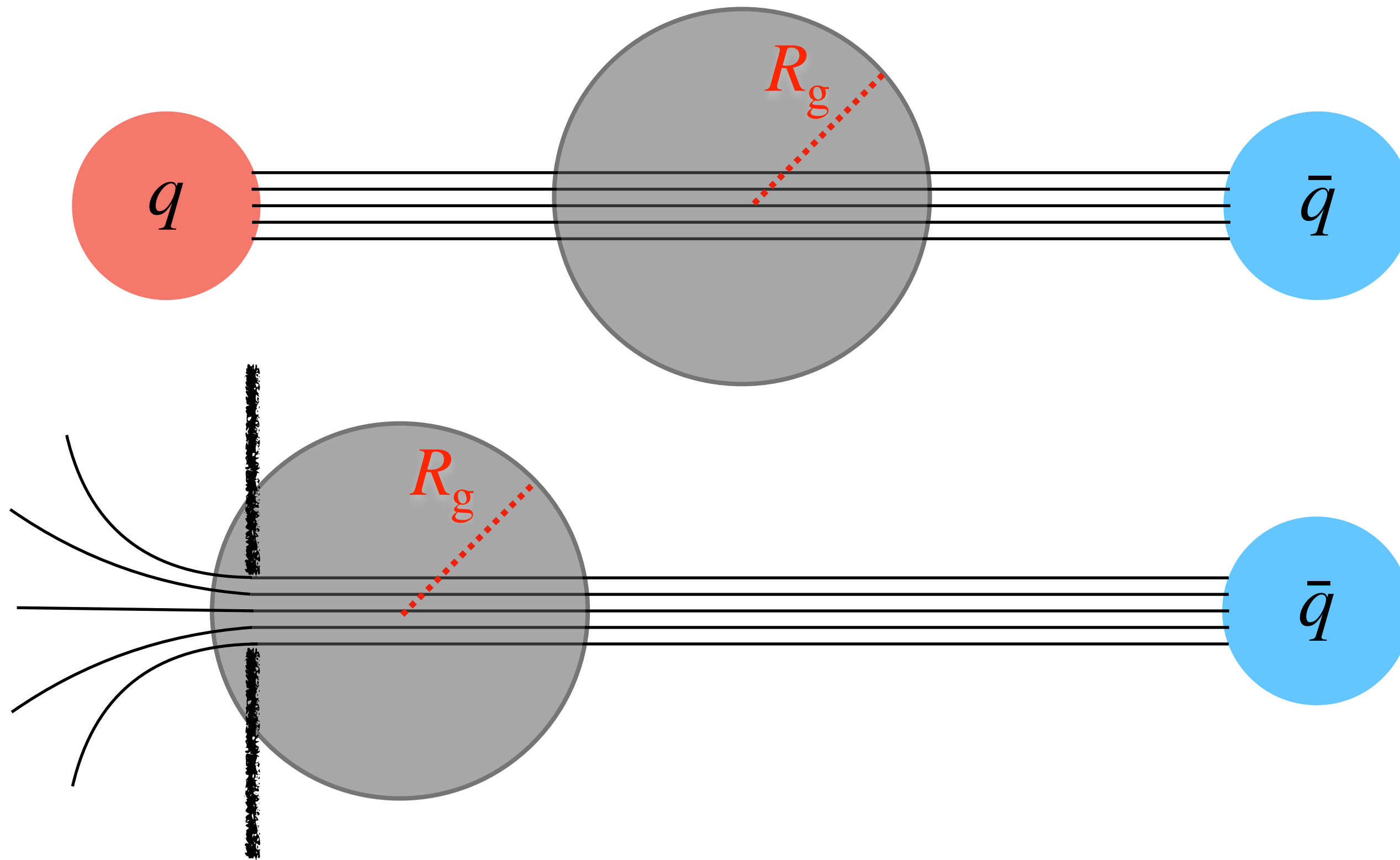
The similar slingshot effect is expected in the “dual” picture when a heavy quark crosses into a confined vacuum of QCD



Field theoretic analogue realisation of a D-brane

Black hole production

The long elongated string stored significant energy: possibility for primordial black holes production, regardless of whether the string ends on a monopole or a domain wall



D o m a i n
(bubble) wall

- Quarks accelerate towards each other $a = \Lambda_c^2/m_q$ and become relativistic

$$E \simeq \Lambda_c^2 l \simeq M_{\text{PBH}}, \quad R_g \gg \Lambda_c^{-1}$$

- Eventually, system might find itself within its own Schwarzschild radius, leading to black hole formation. This dynamics could lead to production of primordial black holes in the early Universe

Overlook

So far we have discussed the case of a monopole slingshot. Can the same effect take place with topological defects of different co-dimension? (YES - Dvali, Bachmaier, Bermudez-Valbuena, MZ, [2309.14195](#))

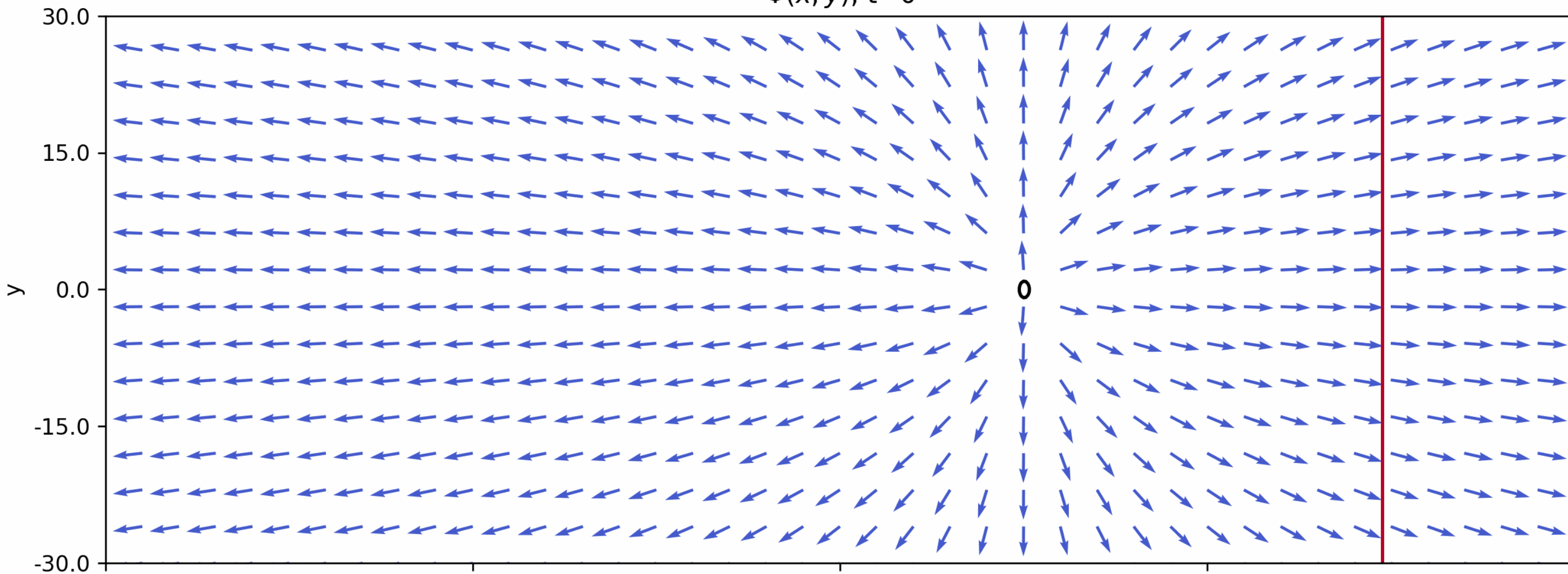
For example, a string would deform the bubble wall on a line (as opposed to the case of a monopole, which deforms it in a point).

Cosmological embedding

Backup

String Slingshot

$\vec{\phi}(x, y), t=0$



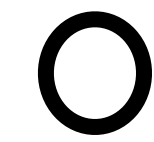
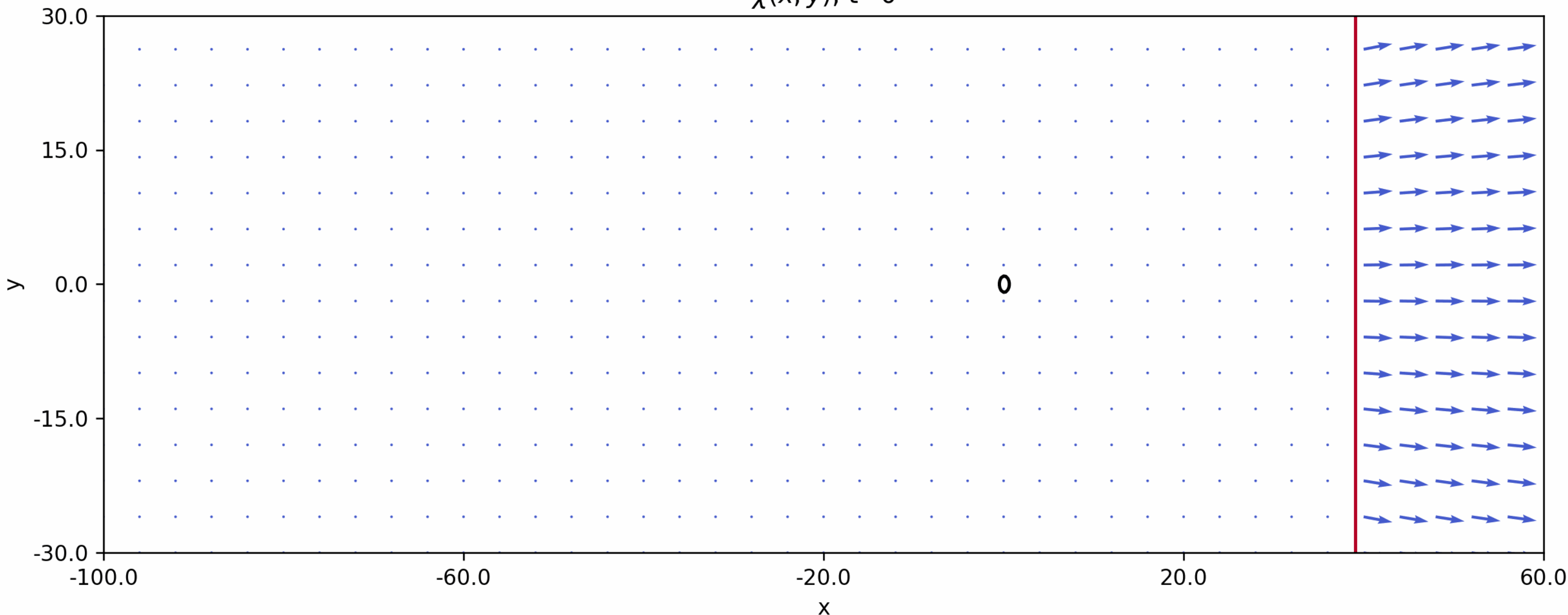
$$SU(2) \rightarrow U(1) \rightarrow 1$$

$$U(1) \times Z_2 \rightarrow Z_2 \rightarrow 1$$

Unconfined region
(Z_2 unbroken)

Confined region
(Z_2 broken)

$\vec{\chi}(x, y), t=0$



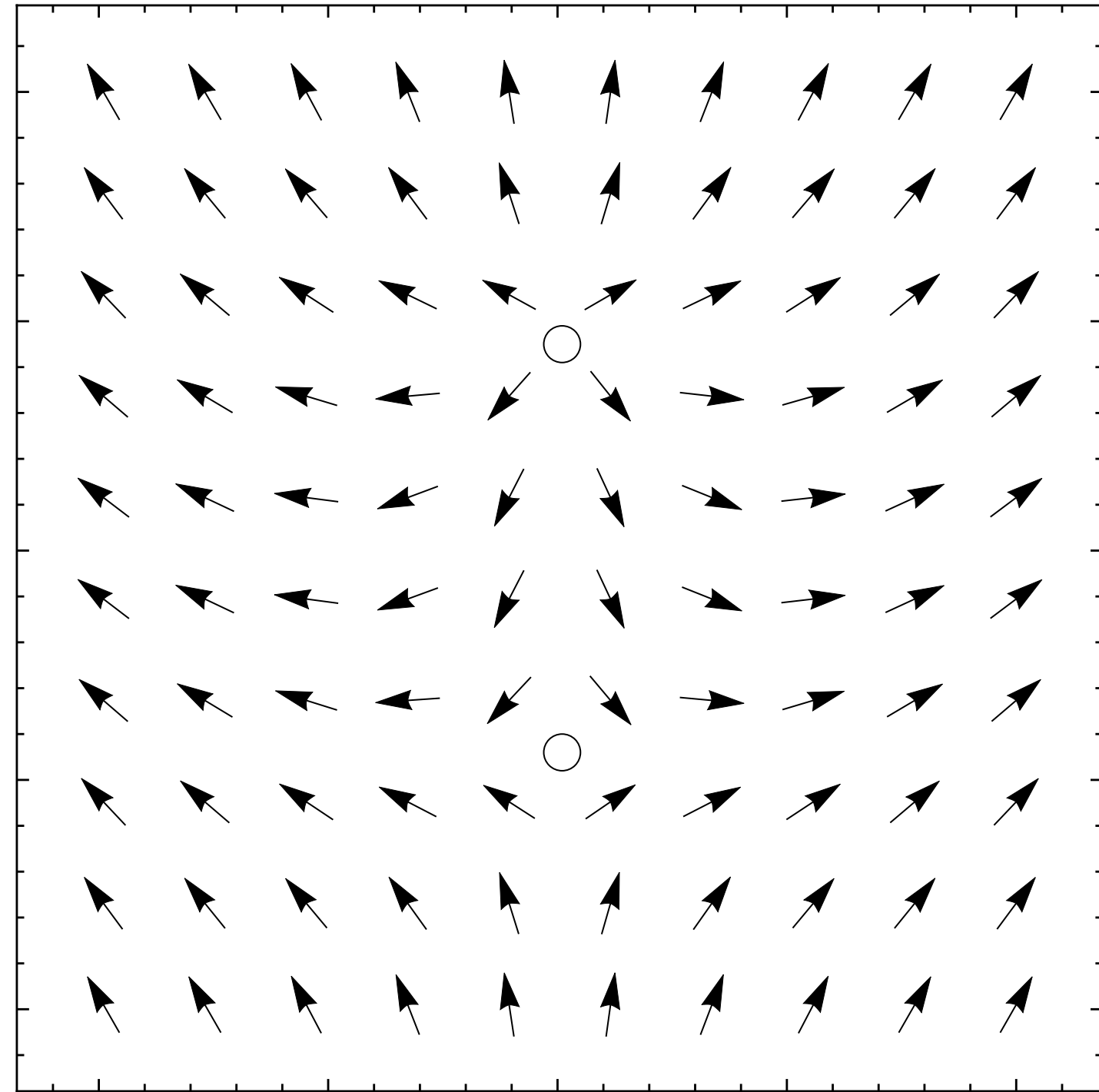
String



$$\mathcal{L} \supset \phi^* \chi^2 + \text{h.c.} \propto \cos(\theta_\phi - 2\theta_\chi)$$

Initial Conditions

$$\varphi^a = h(r_m)h(\bar{r}_m)\hat{\varphi}^a$$



$$D_\mu \hat{\varphi} \Big|_{r \rightarrow \infty} = 0$$

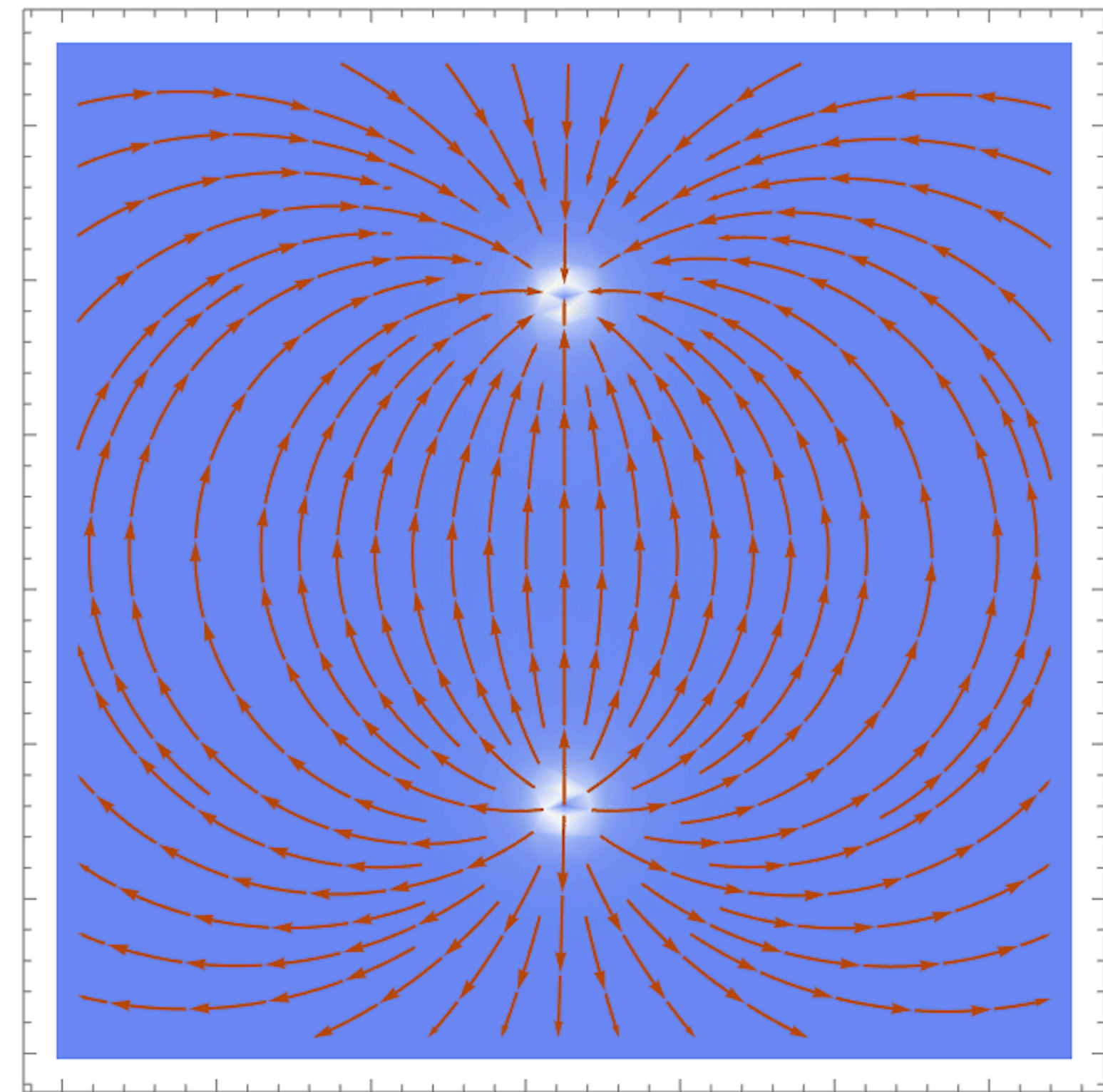


Vachaspati '15

$$W_\mu^a = - (1 - k(r_m))(1 - k(\bar{r}_m))\epsilon^{abc} \hat{\varphi}^b \partial_\mu \hat{\varphi}^c$$

$$F_{\mu\nu} = W_{\mu\nu}^a \hat{\varphi}^a - \epsilon^{abc} \hat{\varphi}^a D_\mu \hat{\varphi}^b D_\nu \hat{\varphi}^c$$

Magnetic field lines



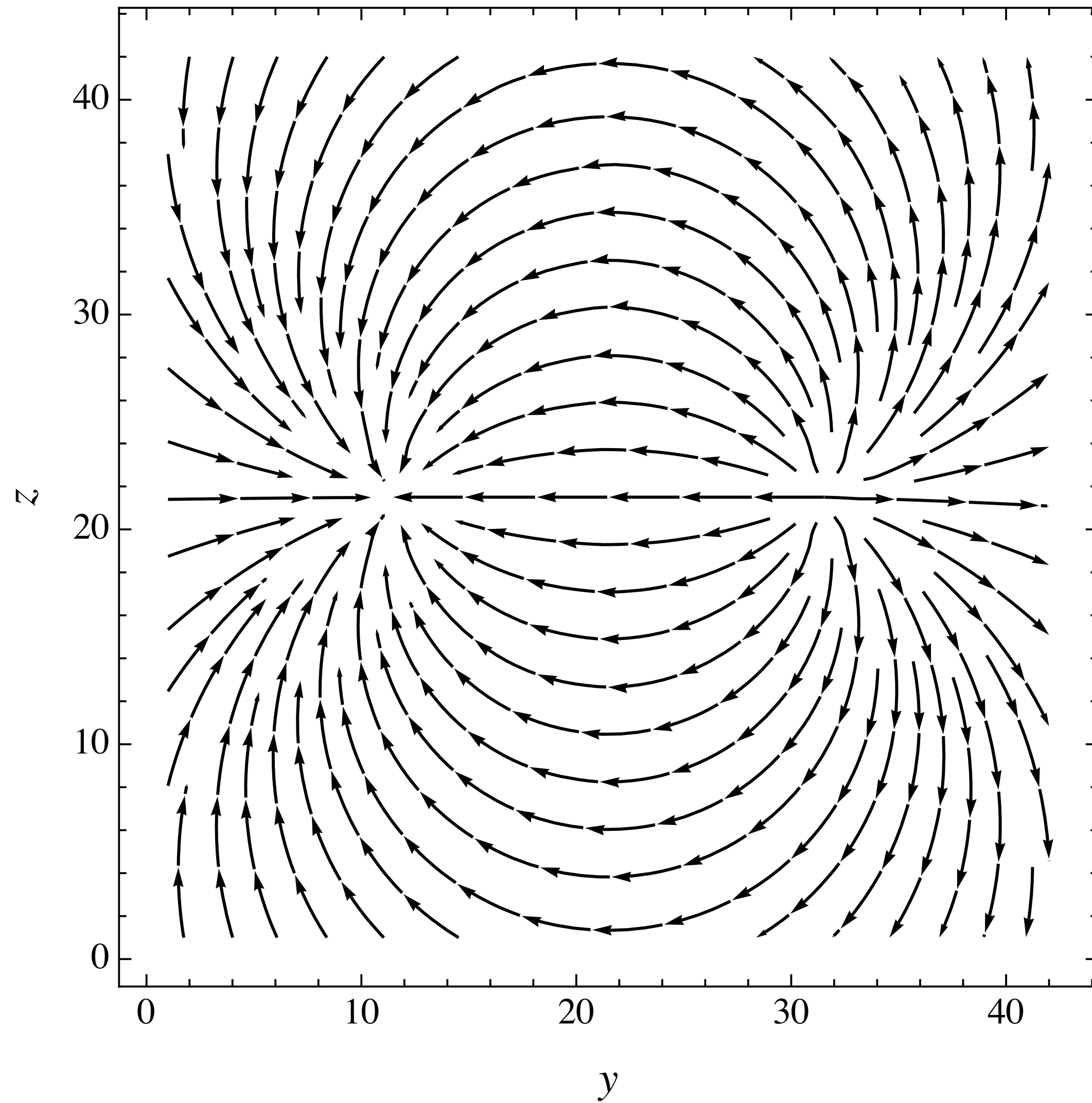
$$\psi = v l(r_{xy}, z) \begin{pmatrix} \sin(\theta/2) \sin(\bar{\theta}/2) e^{i\gamma} + \cos(\theta/2) \cos(\bar{\theta}/2) \\ \sin(\theta/2) \cos(\bar{\theta}/2) e^{i\phi} + \cos(\theta/2) \sin(\bar{\theta}/2) e^{i(\phi-\gamma)} \end{pmatrix}$$

Vachaspati, Field '94

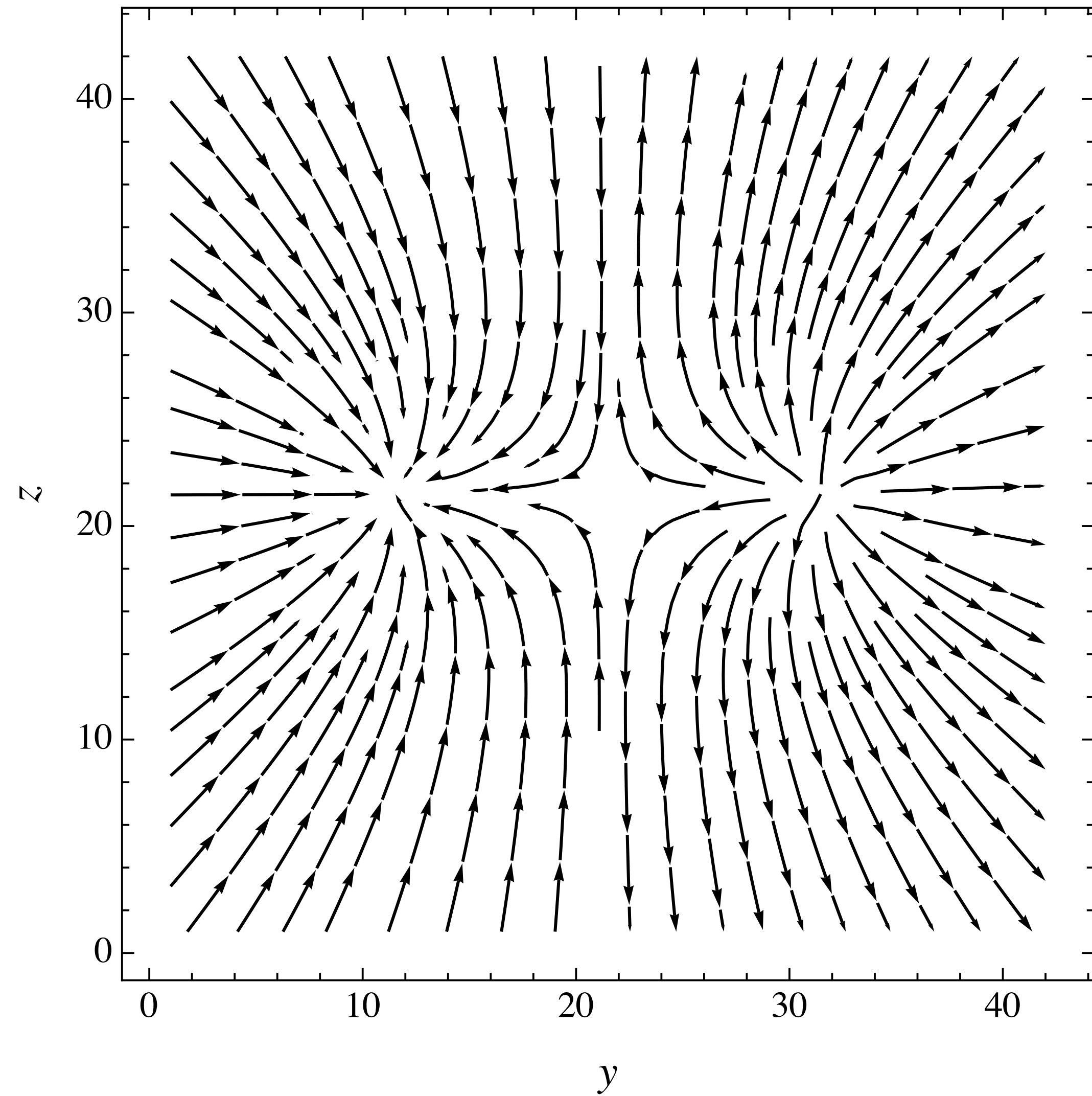
$\gamma =$ twist angle

Adding a twist to the story

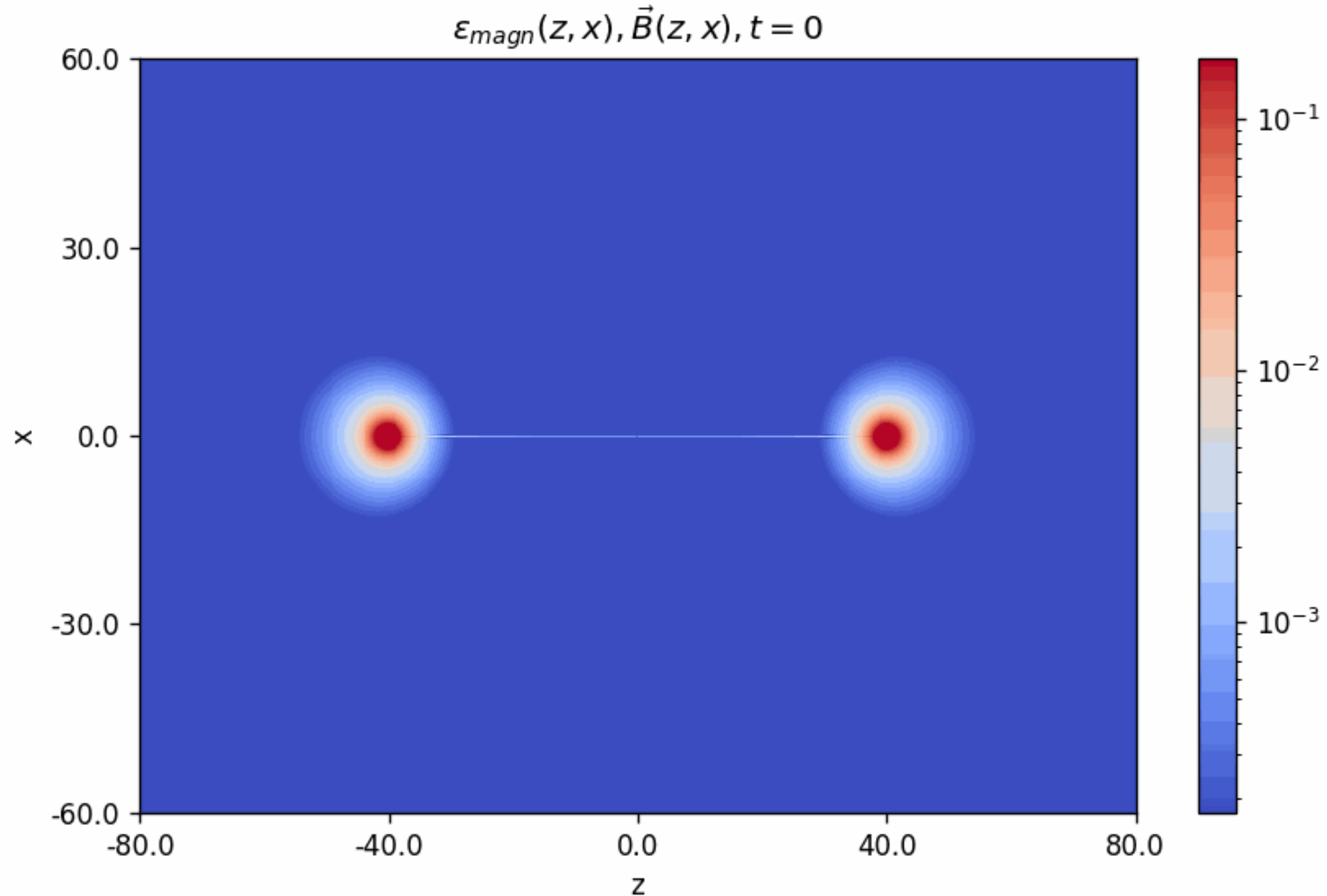
$\gamma = 0$



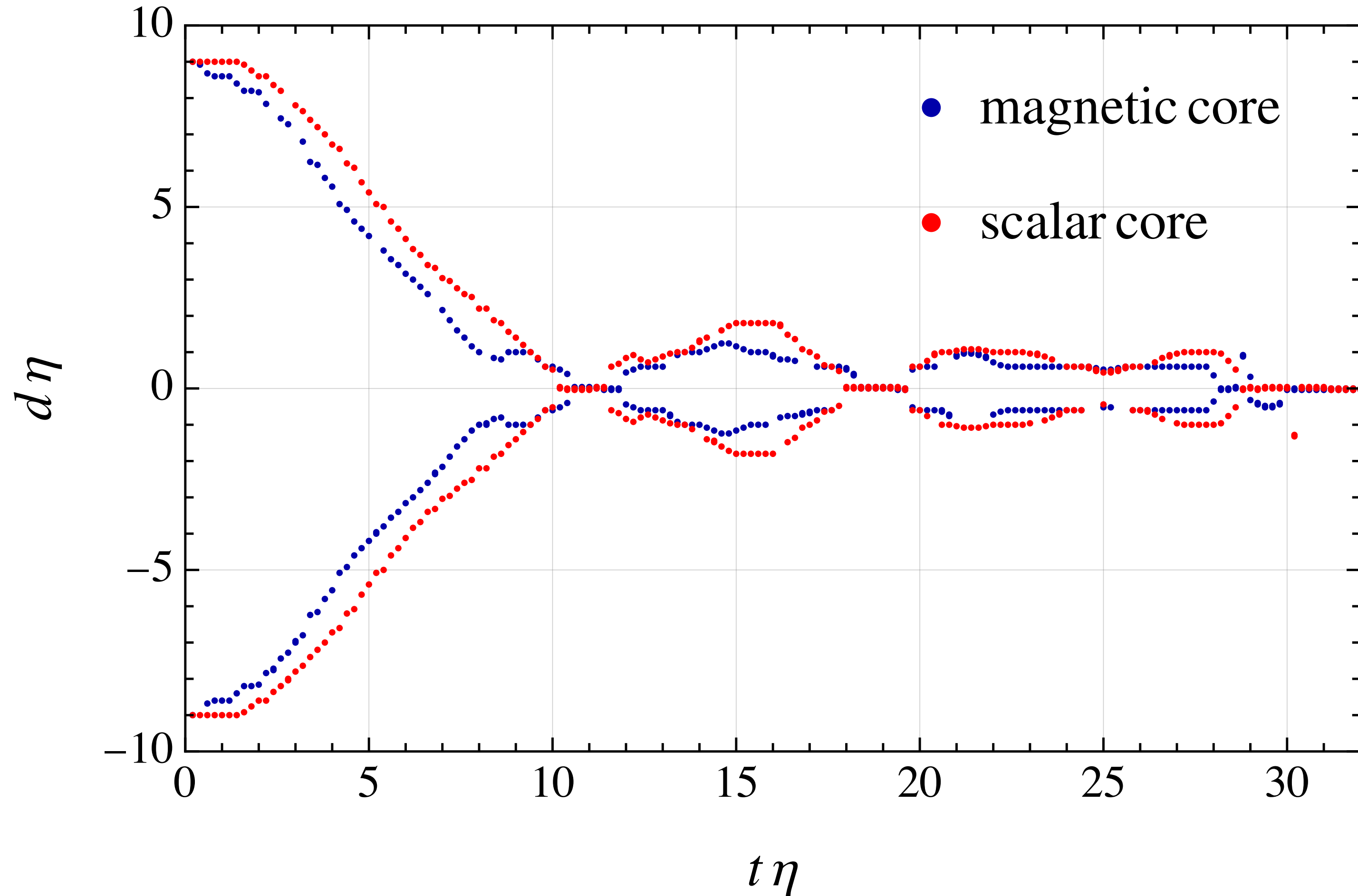
$\gamma = \pi$



Adding a twist to the story



Adding a twist to the story



The configuration is metastable. Simply, the monopoles do not know in which direction to untwist to annihilate. Eventually the instability kicks in, the pair untwist, and it annihilates

More on the dual electric case

Consider $SU(2)$ theory with scalar adjoint with one heavy fermion

Dvali, Shifman hep-th/9612128

$$\mathcal{L} = -\frac{1}{2}\text{Tr} \left(G^{\mu\nu} G_{\mu\nu} \right) + \text{Tr} \left((D_\mu \phi)^\dagger (D^\mu \phi) \right) - U(\phi) + i\bar{Q}\gamma^\mu D_\mu Q - M_Q \bar{Q}Q$$

$$U(\phi) = \lambda \text{Tr} (\phi^2) \left(\text{Tr} (\phi^2) - \frac{v_\phi^2}{2} \right)^2$$

- $\langle \phi \rangle = 0$ theory is in the confined phase - mass gap is generated as in QCD
- $\langle \phi \rangle = v_\phi/\sqrt{2}$ theory is unconfined: there is a residual massless U(1) photon mediating Coulomb interaction

Slingshot expected for $M_Q \gg \Lambda$

Dynamical string formation: phase of confining scalar field - initially randomised

x-y plane at $z=0$

